



## Psychorealism

The realism of the human psyche, expressed through the medium of art and animation.



## Overview

Nonlinear projection


- Cords: Geometry with physical attributes



## dinear perspective

Good approximation of human visual system Conceptually simple and predictable

- Aids depth perception
- Efficient graphics pipeline



## Nonlinear projection

Extend visual range

- Avoid disjoint images for complex scenes
- Artistic expression


## Nonlinear projection model

- $C, M, V$ are the eye-space and perspective, viewport matrices for a linear perspective camera.
- A point in the scene $P$ thus linearly projects under the camera to $\langle x, y\rangle$ in the image at depth $z$ where, $\langle x, y, z>=P C M V$.
- Lets call CMV, E.


## Master and lackey cameras

For $P$ to appear in master camera $b$, as $P$ appears in lackey camera $i$ :

$$
? E_{b}=P E_{i}
$$

$$
P^{\prime}=P C_{i} M_{i} V_{i}\left(C_{b} M_{b} V_{b}\right)^{-1}
$$

$$
A_{i}=C_{i} M_{i} V_{i}\left(C_{b} M_{b} V_{b}\right)^{-1}
$$

## Master and lackey cameras

Given weight $w_{i p}$ for lackey camera $i$ point $P$ deforms to $P^{\prime}$ :

$$
P^{\prime}=P+P\left(w_{i P}\left(A_{i}-I\right)\right)
$$

...and for many lackey cameras

$$
P^{\prime}=P+\sum_{i=1}^{n} P\left(w_{i} P\left(A_{i}-I\right)\right)
$$



## Defining projection weights



Positional



## Examples

## Depth Control



## xamples

## Examples

 yes Depth Control

## Constraints



No Constraints
With Constraints

## Constraints

To see constraint frame $R_{f}$ in lackey as $R_{t}$ in master camera :

$$
E_{i} ? \widehat{E_{b}^{-1}} \quad A_{i}=C_{i} M_{i} V_{i}(\text { Con })\left(C_{b} M_{b} V_{b}\right)^{-1}
$$

... where Con is a constraint matrix that captures the affine transformation that maps $R_{f} E_{i}$ to $R_{t} E_{b}$.
(a) Pillar, $R_{t}$ (lackey view)
(b) Constraint deformed pillar, $R_{t}, R_{f}$ (boss view)

## Constraints

To see constraint frame $R_{f}$ in lackey as $R_{t}$ in master camera :
Con $=\left(\operatorname{Cartesianize}\left(R_{f} C_{i} M_{i} V_{i}\right)\right)^{-1}$ Cartesianize $\left(R_{t} C_{b} M_{b} V_{b}\right)$
...in general Con is defined as an RBF interpolation of multiple constraints per scene object, per camera.



## Shadows



## 

V


## Cords: a physical 3D curve

Cord: A geometric curve primitive that bends and wraps around scene geometry with physical attributes of stiffness and elasticity.

- Desired results are rooted in physics, under precise animator control.


## Motivation

Appealing sparse geometric representations are artistically more challenging than real geometry.



## Cord Detinition

Defined by a guide curve $f(t)$, stiffiness, elasticity, length and 3D scene geometry.
Cord must interactively bend and wrap around geometry in response to animator control of Cord parameters.



















## Cord Algorithm

Initialize Cord to f(0).
Grow the Cord by stepping along f.
if (ray from Cord to fintersects geometry) grow cord to intersection else
grow cord by a stiffness factor along the ray
Adjust Cord to given length, elasticity.

## Cord Analysis

Cord is represented by polyline $\mathrm{p}_{0}, \mathrm{p}_{1}, \mathrm{p}_{2} \ldots$ where

$$
p_{i}=p_{i-1}+\text { stiffness } * s *\left(f(i * s)-p_{i-1}\right) \text { and } p_{0}=f(0) .
$$

We wish to prove that the Cord is a continuous limit curve ( $a=$ stiffiness, $m=t / s$ ) as step-size $s \rightarrow 0$ or $m \rightarrow a$.

$$
p_{m}=f(0) *(1-a * t / m)^{m}+(a * t / m) *\left(\sum_{i=1}^{m} f(i * t / m) *(1-a * t / m)^{m-i}\right)
$$

We show using Riemann sums that:

$$
g(t)=f(0) * e^{-a * t}+a * e^{-a * t} *\left(\int_{0}^{t} f(x) e^{a x} d x\right)
$$

Cords can thus be analytically defined for parametric polynomialiguide curves.


## Wide and thick Cords

- Parameterized sparse geometric representation. -Extension to higher dimensional primitives.





## Acknowledgements



Chris Landreth, Dave Baas.
Byan programming and animation crew.
Support: MITACS, NSERC, CCA, NFB Canada, Seneca College, Alias, Pixar.
http://www.dgp.toronto.edu/~patrick/ryanTech


## Projection Wiadgets

## ...control of artistic perspective using the I-Bar widget.




## Nonlinear projection goals

- Local linear perspective
- Continuous nonlinear projections

Artistic control of composition, projection

- Coherent shading, shadows, lighting
- Interactive and incremental
- Handle complex scenes


